

Process Capability

Process Capability

Process

- Consume Resources and Converts Input into Output

Capability

- is an ability to produce parts within **Specific limit (tolerance)** on a consistent basis



Statistical measurement of a process's ability to produce parts within specified limits on a consistent basis, that is producing good parts.

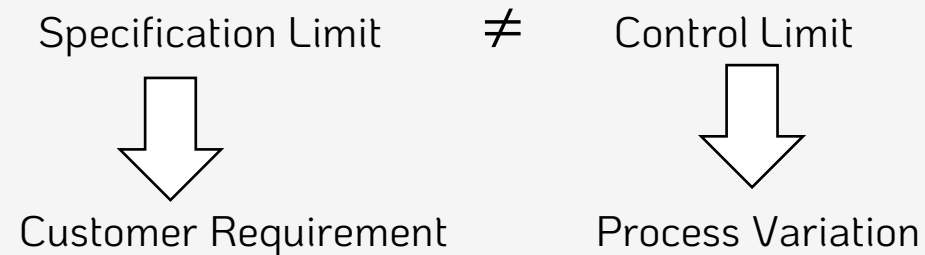
Specification Limits and Control Limit

Specification Limit

- Represent process variation and indicate when your process is in control, defined by **USL** (Upper Specification Limit) and **LSL** (Lower Specification Limit)

Control Limit

- **UCL** (Upper Control Limit) and **LCL** (Lower Control Limit) are based on **random variation** in the process.



The Basic Concept

When the manufacturing process is being defined, **your goal is to ensure that the parts produced fall within the Upper and Lower Specification Limits** (USL, LSL). Process Capability measures how consistently a manufacturing process can produce parts within specifications.

The basic idea is very simple. You want your manufacturing process to:

- (1) be centered over the Nominal desired by the design engineer, and
- (2) with a spread narrower than the specification width.

The Basic Calculations

Before we get into the detailed statistical calculations, let's review the high-level steps:

1: **Plot the Data:** Record the measurement data, and plot this data on a run-chart and on a histogram.

2: **Calculate the Spec Width:** Plot the Upper Spec Limit (USL) and Lower Spec Limit (LSL) on the histogram, and calculate the Spec Width as shown below.

$$\text{Spec Width} = \text{USL} - \text{LSL}$$

3: **Calculate the Process Width:** Similarly, we will also calculate the Process Width. The simplest way to think about the process width is "the difference between the largest value and the smallest value this process could create".

$$\text{Process Width} = \text{UCL} - \text{LCL}$$

4: **Calculate Cp (Capability Index) :** Calculate the capability index as the ratio of the spec width to the process width.

$$\text{Cp} = \text{Spec Width} / \text{Process Width}$$

The Basic Calculations

Calculate Cp (Capability Index) : Calculate the capability index as the ratio of the spec width to the process width.

$$Cp = \text{Spec Width} / \text{Process Width}$$

$$Cp = \text{USL} - \text{LSL} / 6\sigma$$

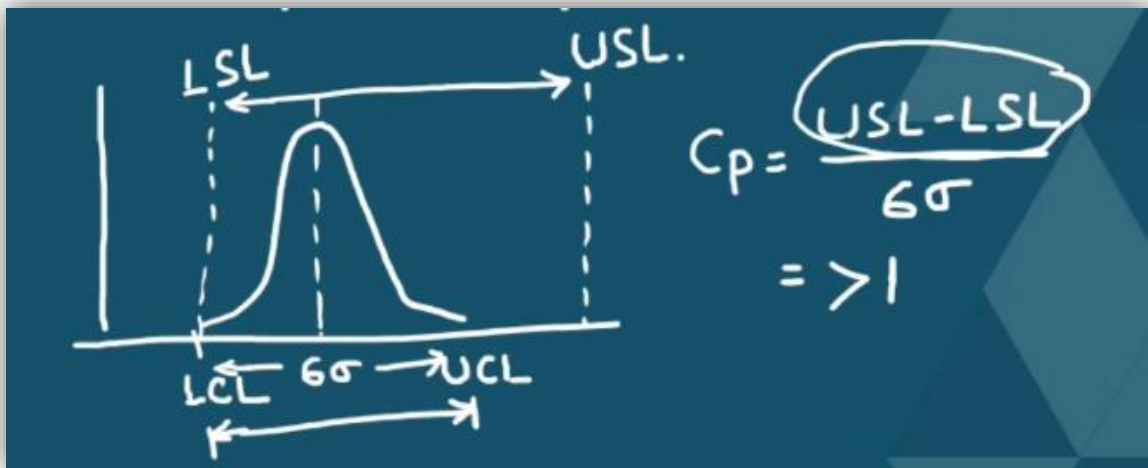
Process Capability, condition should be met:

- Sample to represent the population
- Normal distribution of Data
- The process must be in statistical control
- Sample size must be sufficient

The Basic Calculations

Calculate Cpk (Process performance) : is used to summarize how a process is running relative to its specification limit.

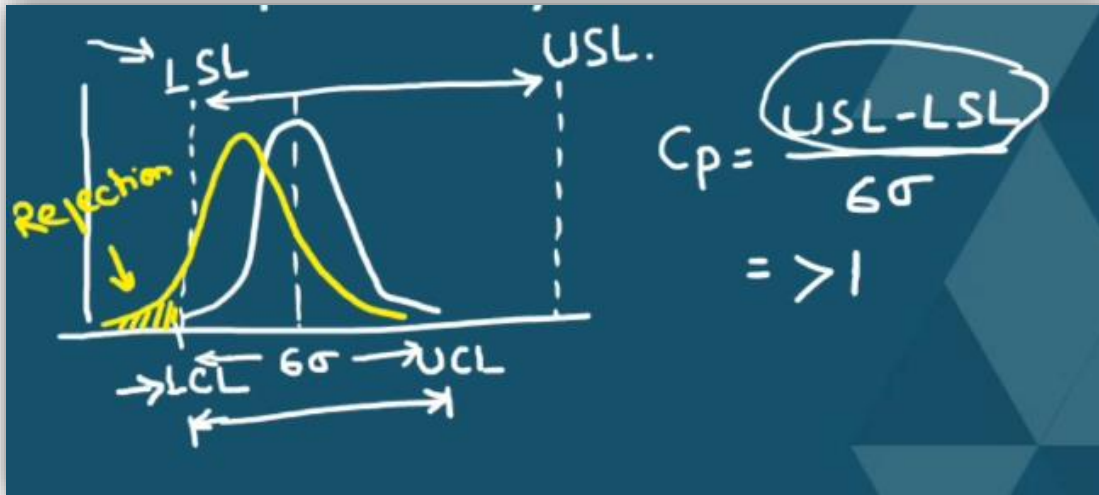
Why we need Cpk ? Let's see the example below:



Here LSL and LCL are just at the same point. Any fluctuation on the lower side would put this product out of Spec.

The Basic Calculations

Why we need Cpk ?

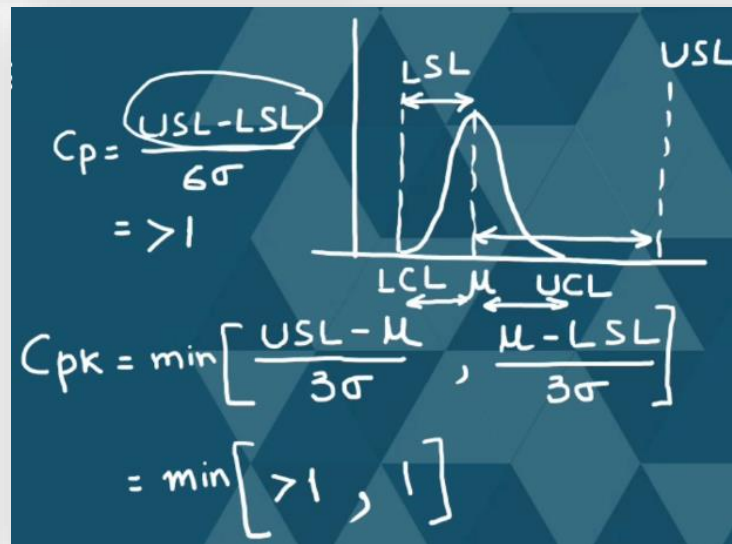
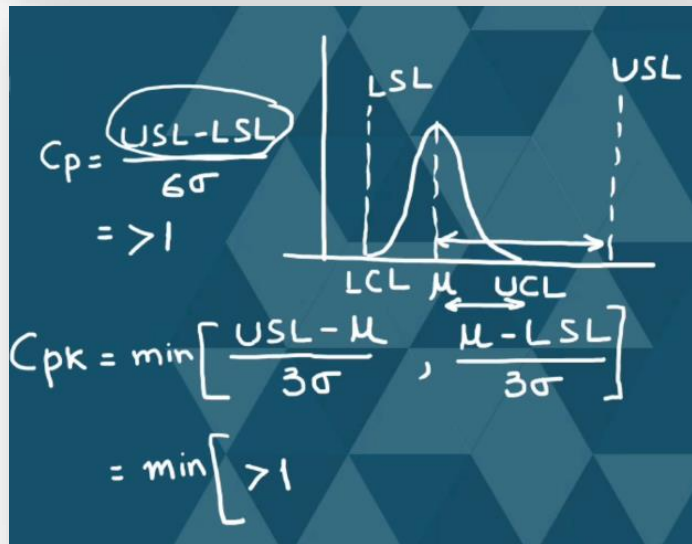


When the curve moves little bit to left over time then we get products rejected. **Cp doesn't tell you that.** So, to take care of that, we have another parameter, which is **Cpk**

The Basic Calculations

How to calculate **Cpk**?

$$C_{pk} = \min \left[\frac{USL - \mu}{3\sigma}, \frac{\mu - LSL}{3\sigma} \right]$$



$$C_{pk} = 1$$

The Basic Calculations

How about in terms of Cpk ?

Cpk < 1.00 (Poor, incapable)

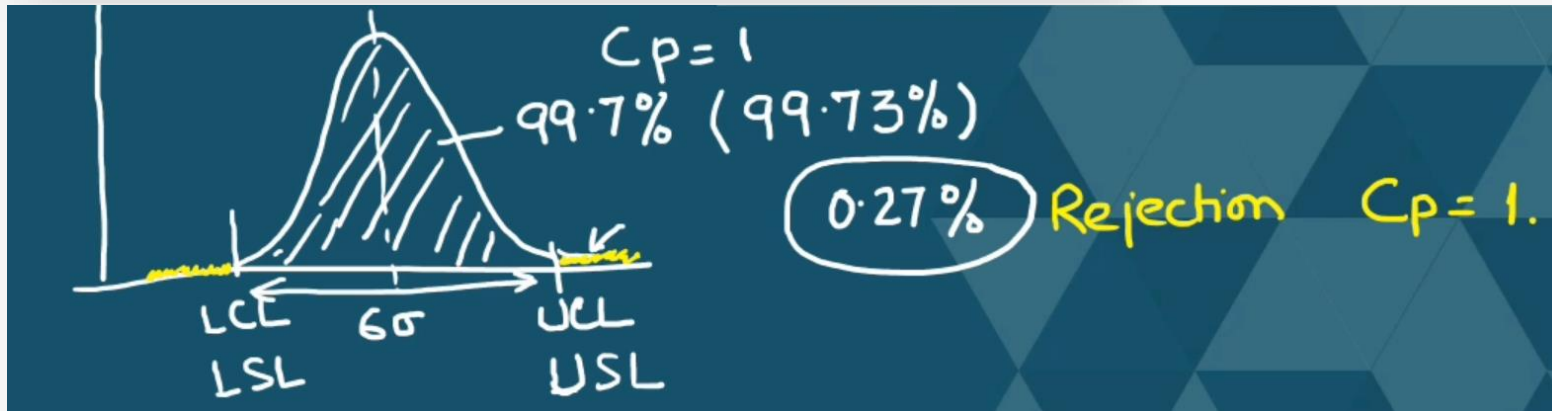
1.00 < **Cpk** < 1.67 (Fair)

Cpk > 1.67 (Excellent, Capable)

Cpk = 2 for a 6σ process (i.e. a 6 sigma process)

Process Capability Vs Rejection

| | | | | |
|---------|------------|------------|-------------|-------------|
| USL-LSL | 6 σ | 8 σ | 10 σ | 12 σ |
| Cp | 1.00 | 1.33 | 1.66 | 2.00 |
| Rejects | 0.27 % | 64 ppm | 0.6 ppm | 2 ppb |




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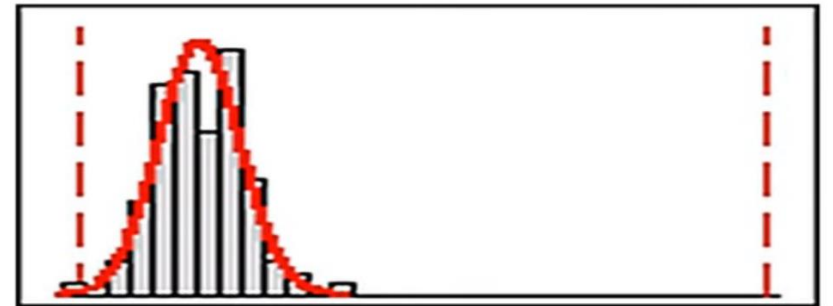
Cp value increase 

Rejection Rate decrease 

Process Capability Vs Rejection

Cpk is preferred to Cp because it measure both process location and process standard deviation.

$$Cpk = \min \{CPL = 0.96, CPU = 4.56\} = 0.96$$



Cpl and Cpu is called One sided Process Potential

Process Capability Analysis Vs Process Performance Analysis

[Potential] Process Capability Analysis (Cp, Cpk):

A process capability study uses data from a sample to PREDICT the ability of a manufacturing process to produce parts conforming to specifications. This prediction enables us to "qualify" a new manufacturing process as being fit for use in production. The index Cp provides a measure of potential process capability i.e. how well a process can perform if there is no change in the underlying process conditions.

Cpk uses "s-short-term" to predict the behavior of the process.

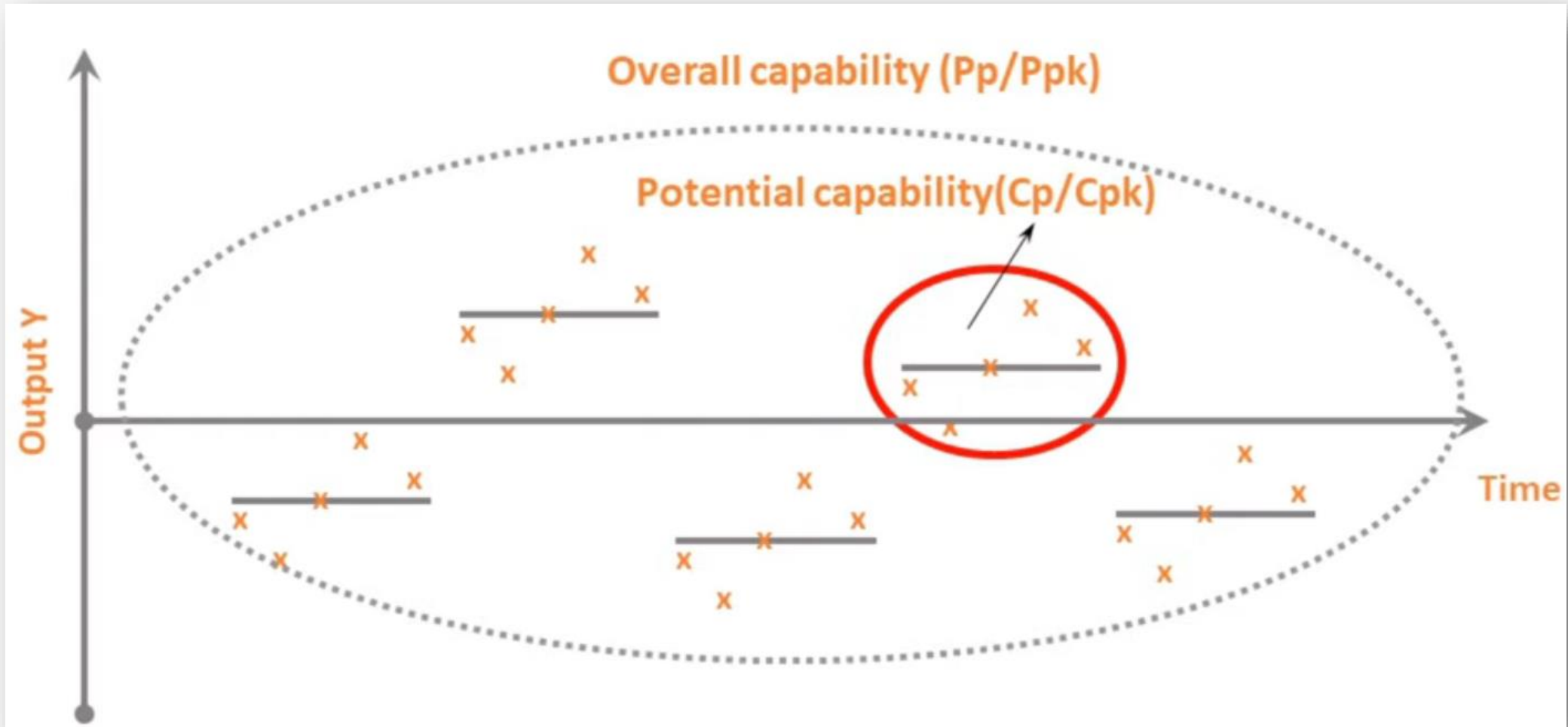
[Actual] Process Performance Analysis (Pp, Ppk):

A process performance study is used to EVALUATE a manufacturing process and answers the question: "how did the process actually perform over a period of time?" This is a historical analysis rather than a predictive analysis, but can still be used to drive process improvements.

Ppk uses "s-long-term" to evaluate the behavior of the process.

If the process is stable, $Ppk = Cpk$, i.e. the actual performance will match the predicted potential performance. However, if the process is unstable; i.e. if it shifts or drifts over time; you will find $Ppk \ll Cpk$.

Process Capability Analysis Vs Process Performance Analysis



Process Capability Analysis Vs Process Performance Analysis

$$C_p = (USL - LSL) / (6\sigma_{\text{within}})$$

$$C_{pU} = (USL - \text{mean}) / (3\sigma_{\text{within}})$$

$$C_{pL} = (\text{mean} - LSL) / (3\sigma_{\text{within}})$$

$$C_{pk} = \min \{C_{pU}, C_{pL}\}$$

Potential Capability

$$P_p = (USL - LSL) / (6\sigma_{\text{overall}})$$

$$P_{pU} = (USL - \text{mean}) / (3\sigma_{\text{overall}})$$

$$P_{pL} = (\text{mean} - LSL) / (3\sigma_{\text{overall}})$$

$$P_{pk} = \min \{P_{pU}, P_{pL}\}$$

Overall Capability

- Calculations for C_p and P_p are similar

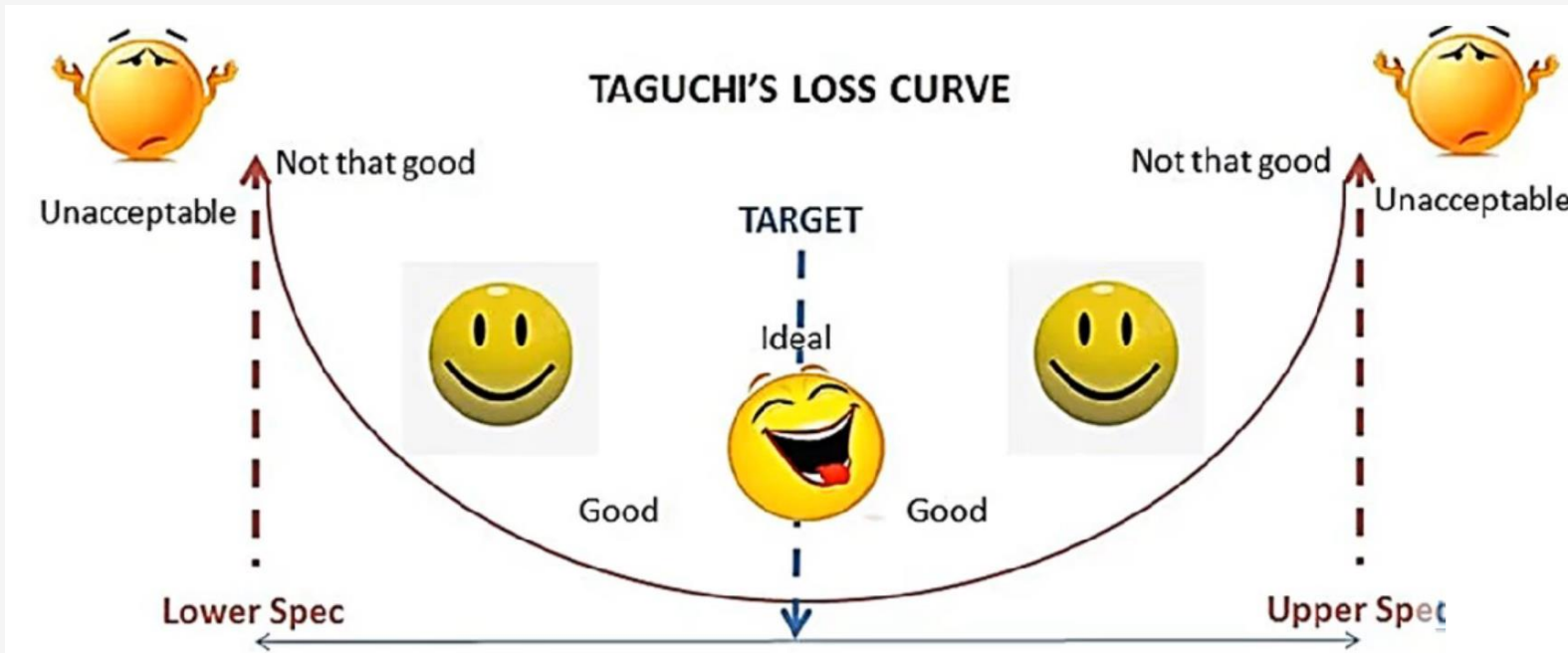
Difference between Cpk & Ppk

Cpk is calculated using “within” standard deviation, while

Ppk is using “overall” standard deviation.

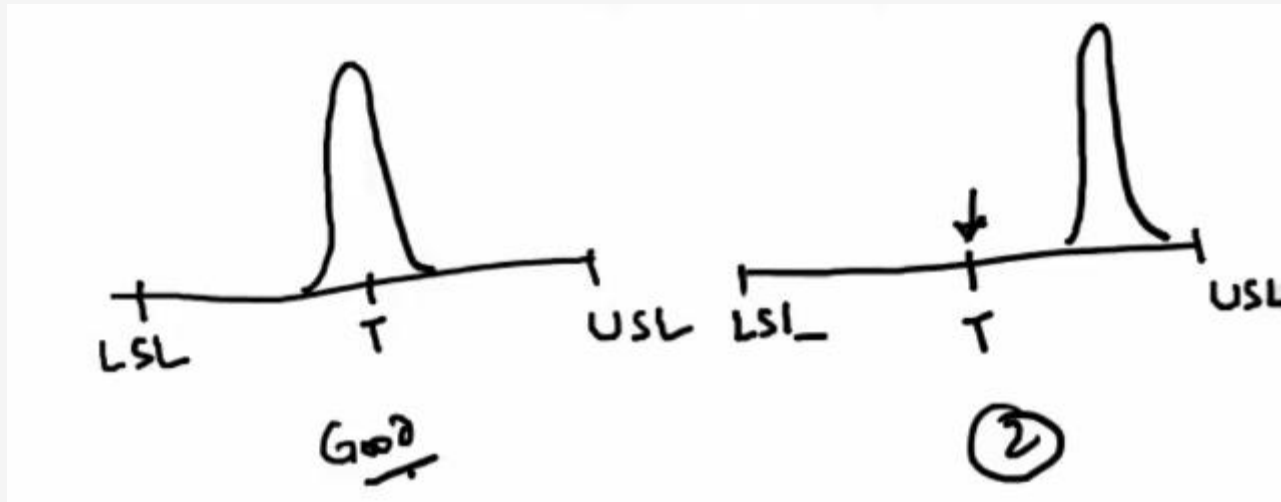
The Basic Calculations

Cpm : focus on how well the process mean correspond to process target, which may or may not be in between spec. limit.



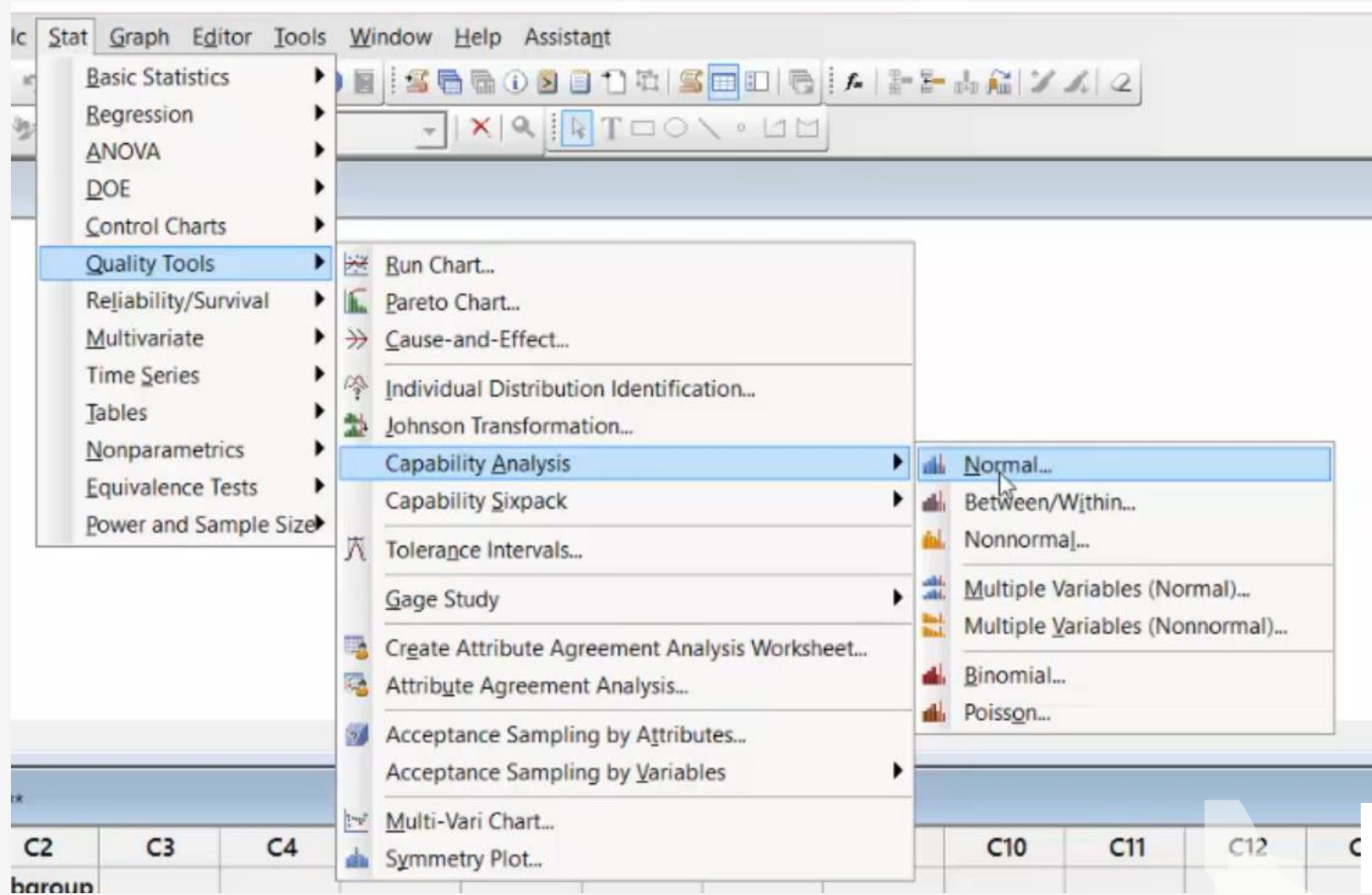
The Basic Calculations

C_{pm} : focus on how well the process mean correspond to process target, which may or may not be in between spec. limit.

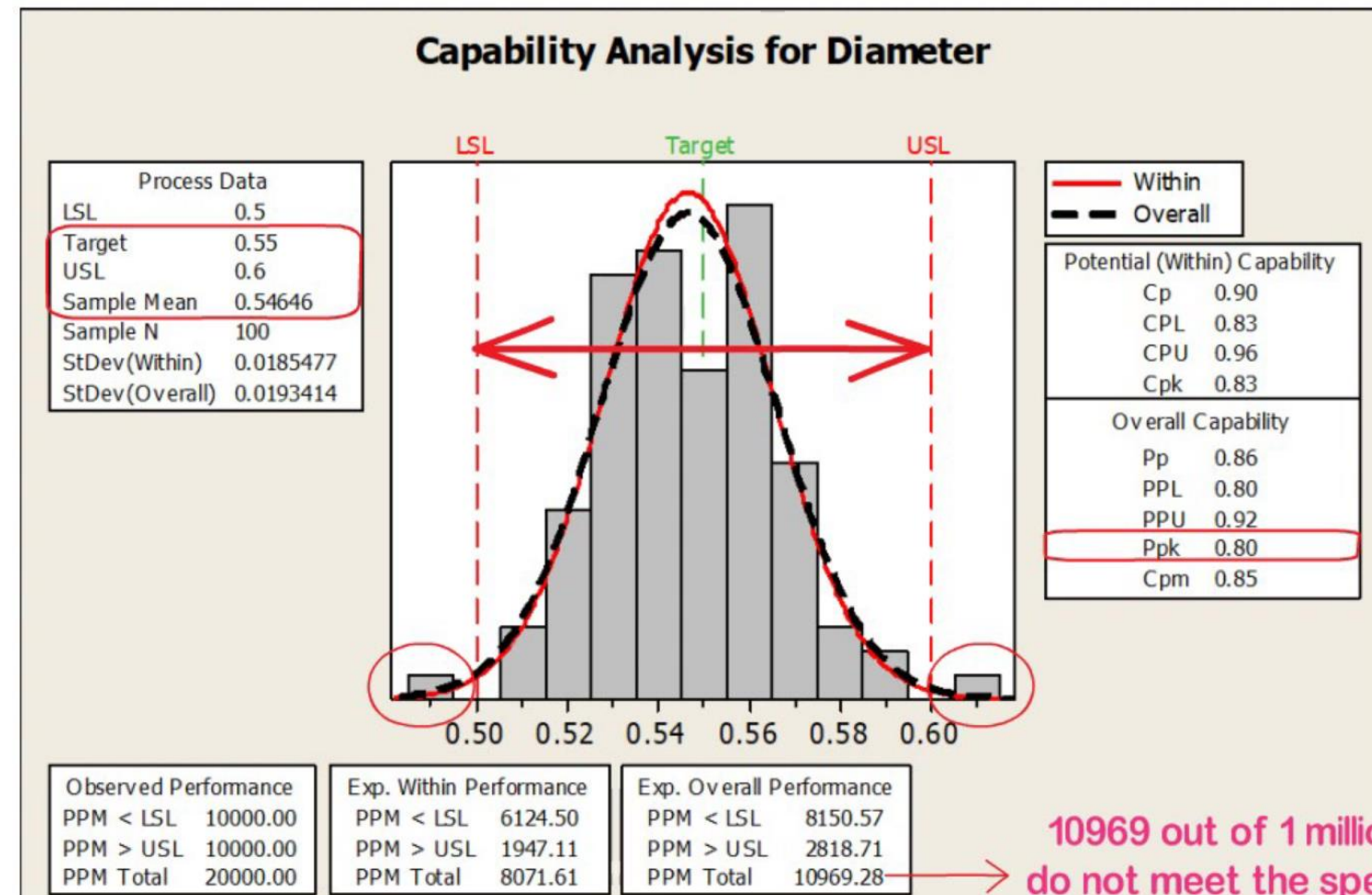


$$C_{pm} < C_p$$

Minitab and Calculating Process Capability



Minitab and Calculating Process Capability



-The manufacturer is not meeting customer's requirements and should improve its process by reducing process variation

-The manufacturer must improve the process by

- reducing variability and
- centering the process on the target

10969 out of 1 million cables do not meet the specifications